

**Force**

**Motion**

**Q39**

# Chapter 4 Forces & Newton's Laws

- Kinematics
  - study of motion
- Mechanics
  - forces that cause the motion

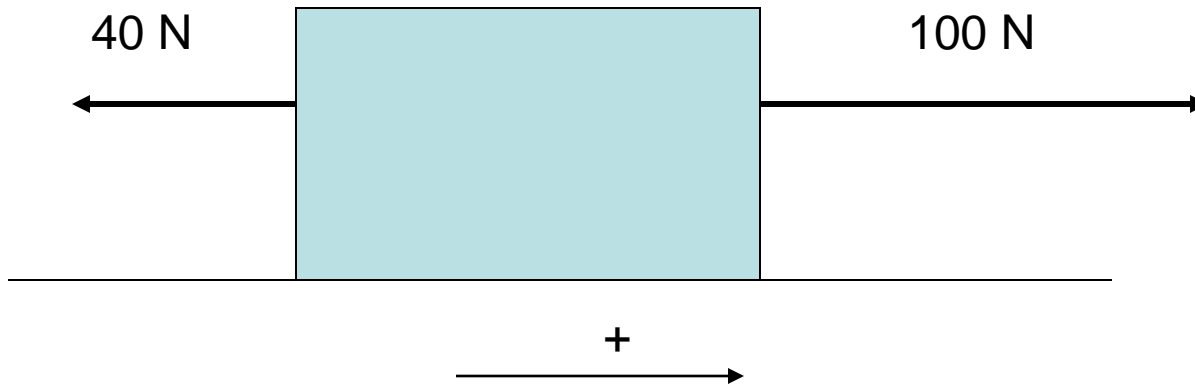
# Force

- A force is exerted when two “systems” interact.
- Contact forces
  - surfaces in contact
  - rope or cable attached to an object
- Non-contact “action-at-a-distance” forces
  - fields exert gravitational, electric, magnetic forces
- Forces cause, or try to cause, a change in the state of rest or motion of an object
- Forces cause object to change velocity = accelerate
- Vector quantity

# Net Force

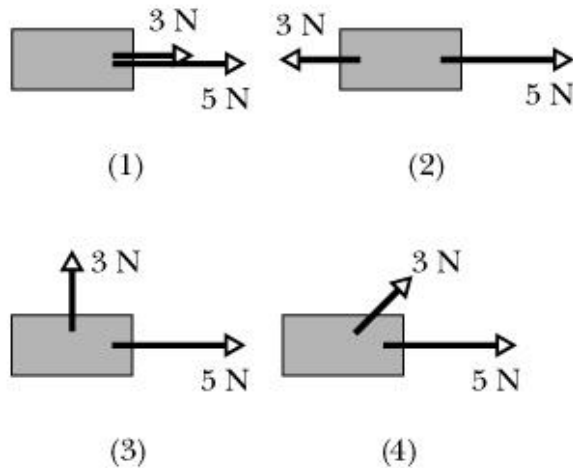
- $\Sigma F$  “sigma F” = net force
  - vector sum of forces acting on object
- Paycheck example
  - do you receive a gross or net paycheck?

$$\Sigma F = 100 + (-40) = 60 \text{ N}$$



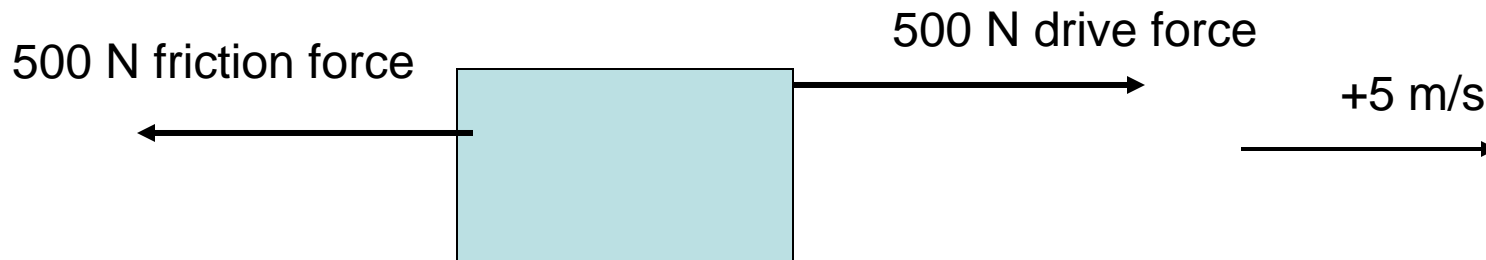
# Applied force vs Net force

- Net force is a vector sum of the actual applied forces.



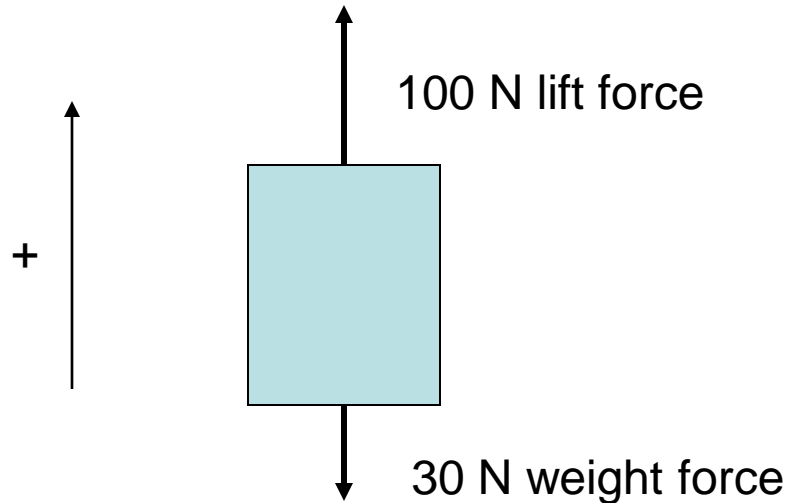
# Balanced Forces

- Forces of equal magnitude acting on an object in opposite directions
- $\Sigma F = 0$  (does not mean no forces act)
- Object moves with constant velocity
  - stays at rest or at constant speed in a straight line



# Unbalanced Forces

- Opposing forces of different magnitudes that do not 'cancel each other out'



$$\Sigma F = 70 \text{ N}$$

- unbalanced forces cause acceleration in the direction of the unbalanced net force

# Inertia

- Tendency of an object to remain at rest or in motion at a constant velocity
- The resistance of an object to a change in its state of rest or motion
- MASS is a measure of inertia



Penny  
(0.003 kg)



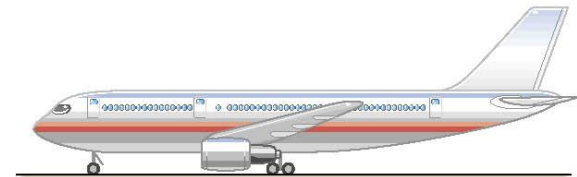
Book  
(2 kg)



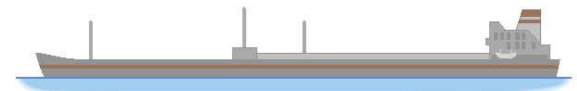
Bicycle  
(15 kg)



Car  
(2000 kg)



Jetliner  
( $1.2 \times 10^5$  kg)



Supertanker  
( $1.5 \times 10^8$  kg)



# Newton's 1<sup>st</sup> Law of Motion

- An object's inertia will keep it at rest or in motion at a constant speed in a straight line (= constant velocity) unless acted on by a net force.
- Law of Inertia
- $\Sigma F = 0$

# Newton's 2<sup>nd</sup> Law of Motion

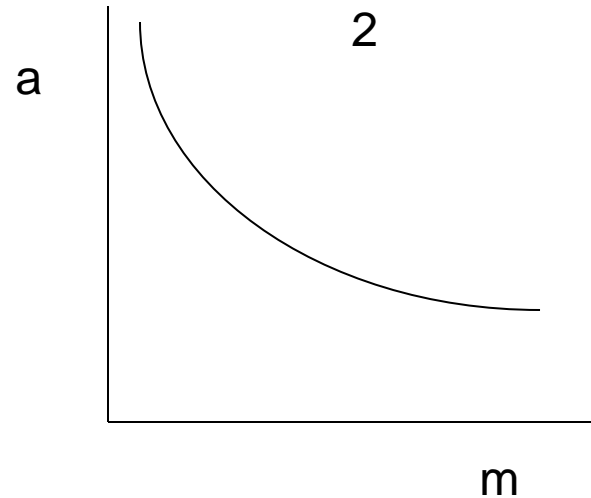
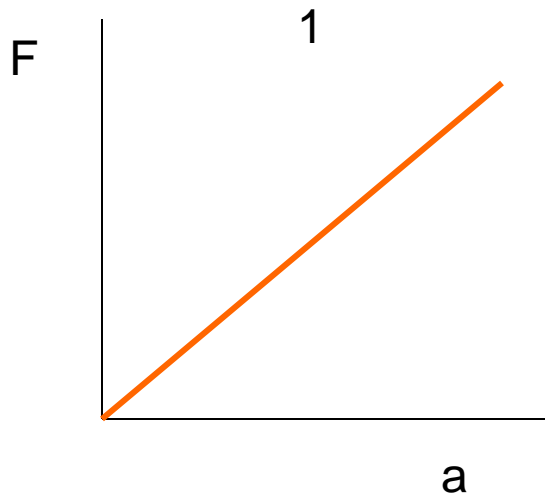
- When a net force acts on an object it accelerates in the direction of the net force.
- Acceleration is *directly* proportional to the magnitude of the net force applied to a constant mass
- Acceleration is *inversely* proportional to the mass of the object for a constant net force
- $a = \frac{\Sigma F}{m}$

$$\Sigma F = (m)(a)$$

left side of 2<sup>nd</sup> law  
is vector sum

right side is a mathematical  
= product of mass and  
acceleration value

- Which of Newton's Laws is represented by the graphs below?



Newton's 2<sup>nd</sup> Law

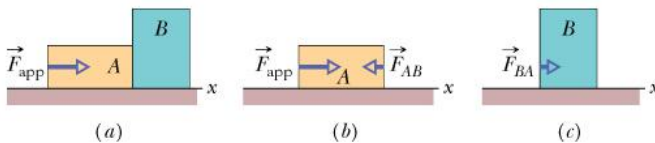
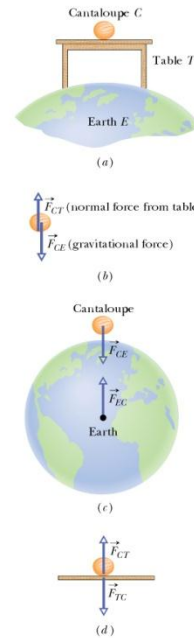
slope of graph 1 = constant mass that force is applied to

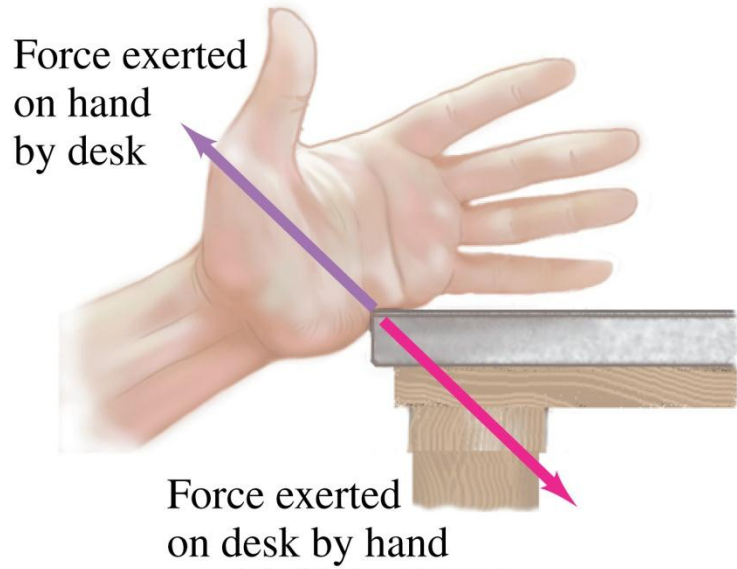
constant force applied to increasing mass in graph 2

definition of "inertial mass" – resistance to acceleration

# Forces come in pairs

- 3<sup>rd</sup> Law
- action-reaction force pairs
  - never act on the same object

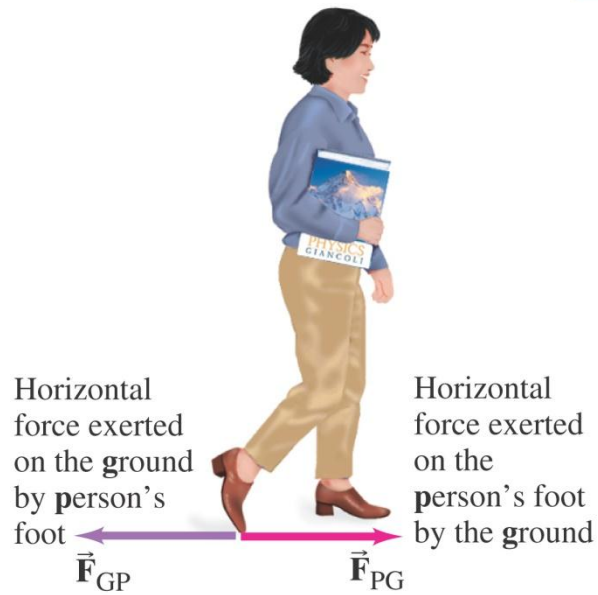




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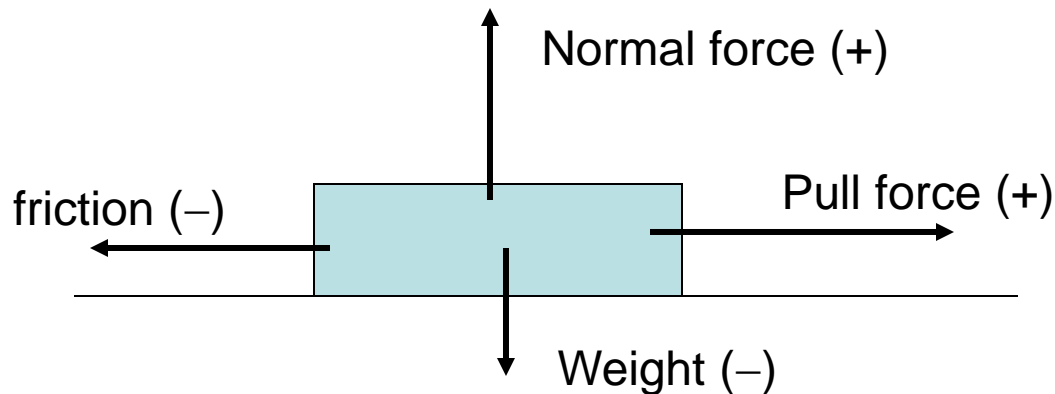
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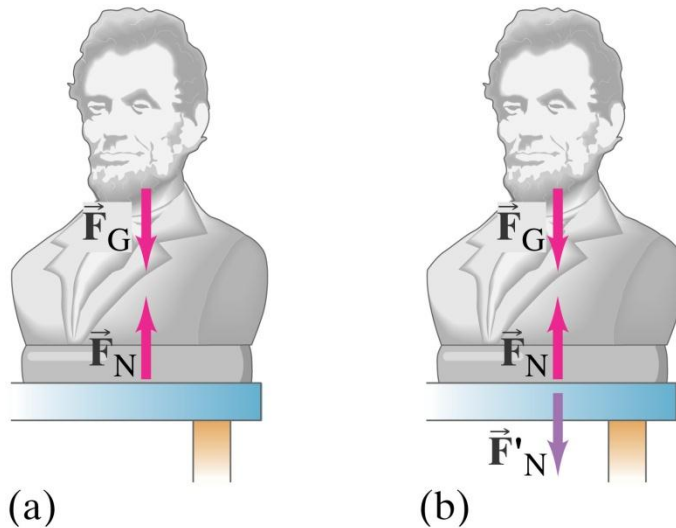
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# Free Body Diagram

- simple drawing of the object in a problem
- ALL forces acting on the object are shown with arrows for force vectors.
- Tail of arrow is attached to object
- Arrow points in direction of force and is labeled correctly with name or abbreviation
- Signs are important in problem solving

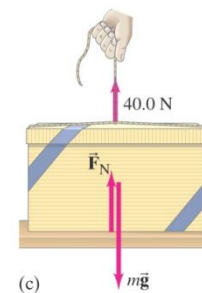
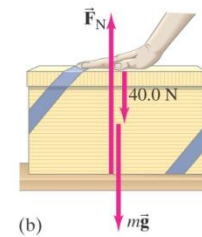
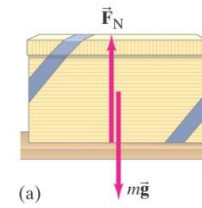


# Normal force and gravitational force



$F_G$  gravitational force

- force exerted on a mass when in a gravity field created by another mass
- Weight in Newtons = (mass in kg) •  $g$  =  $m \cdot 9.8$  at Earth's surface



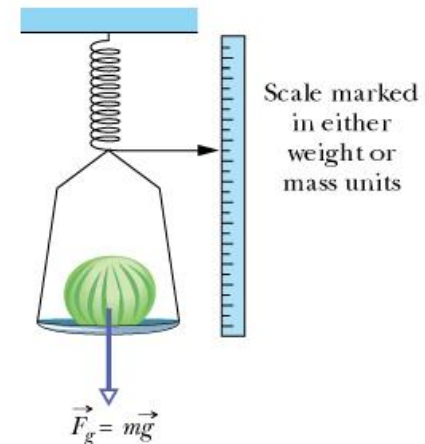
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Normal force not always equal to the weight of an object

$\Sigma F = 0$  to solve for  $F_N$

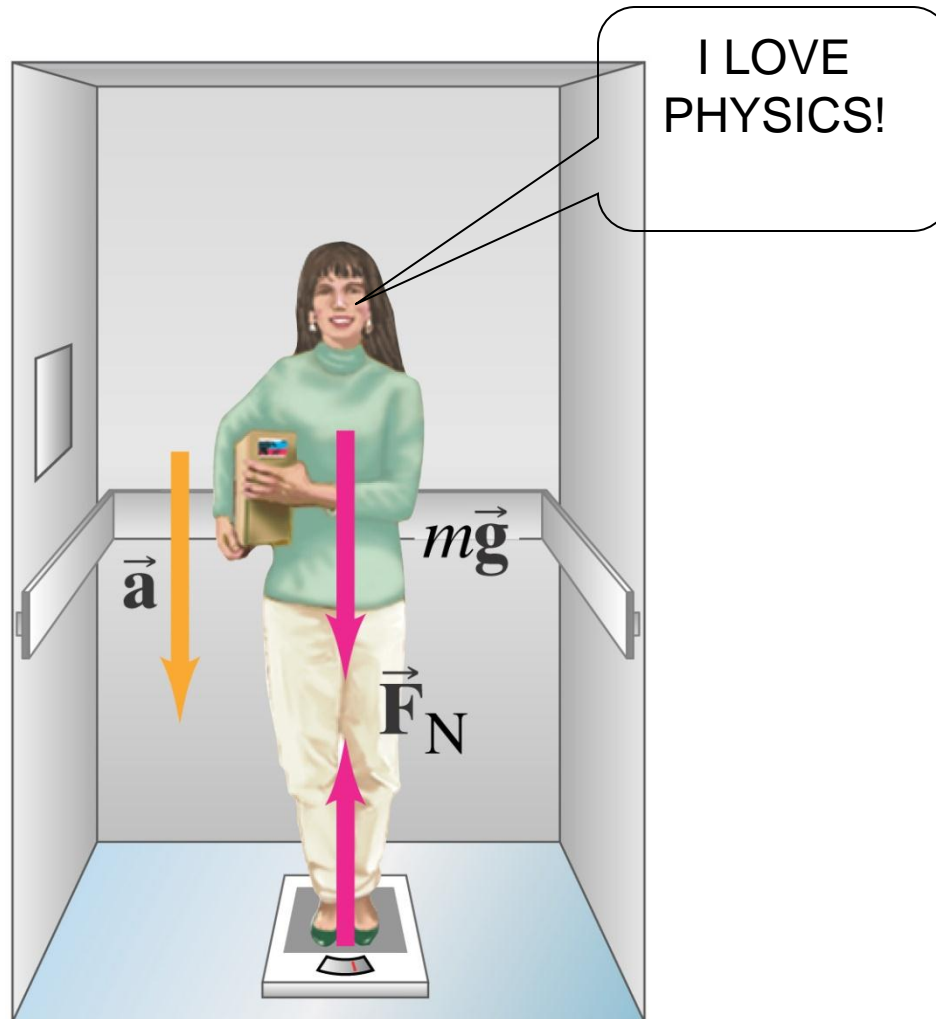
# Mass vs Weight

- Mass (kg) as source of gravitational forces
  - constant at all points
  - measure of object's inertia
- Weight ( $F_g$ ) =  $mg$  (N)
  - varies with strength of gravitational attraction

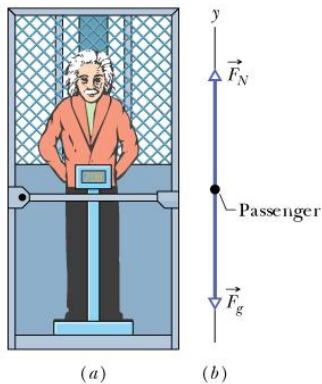




# Elevator Problems



- Accelerating up or down will change the “apparent” gravitational acceleration rate  $g$



Al's weight scale reading ( $F_N$ ) is his apparent weight

$$F_N - F_g = ma_{\text{elev}}$$

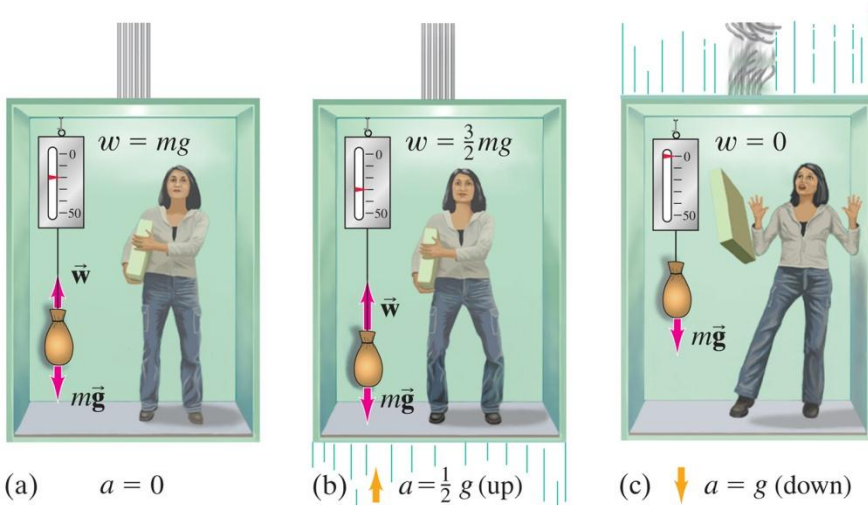
$$F_N = m(g + a_e)$$

( $a_e = +$  if up and  $-$  if down)

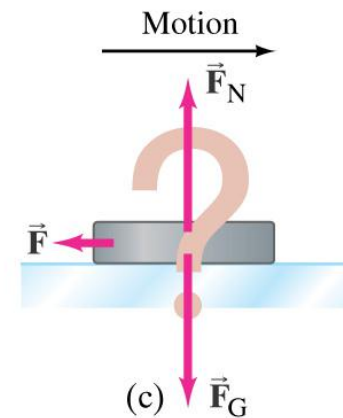
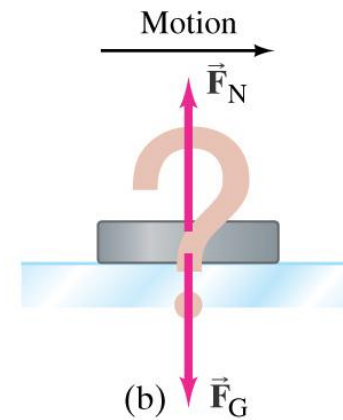
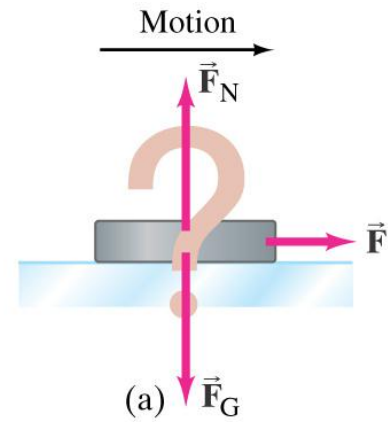
Accelerating up = heavier

Accelerating down = lighter

Free fall down: apparent weight = 0

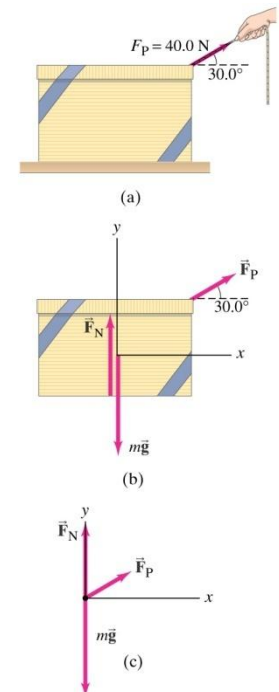
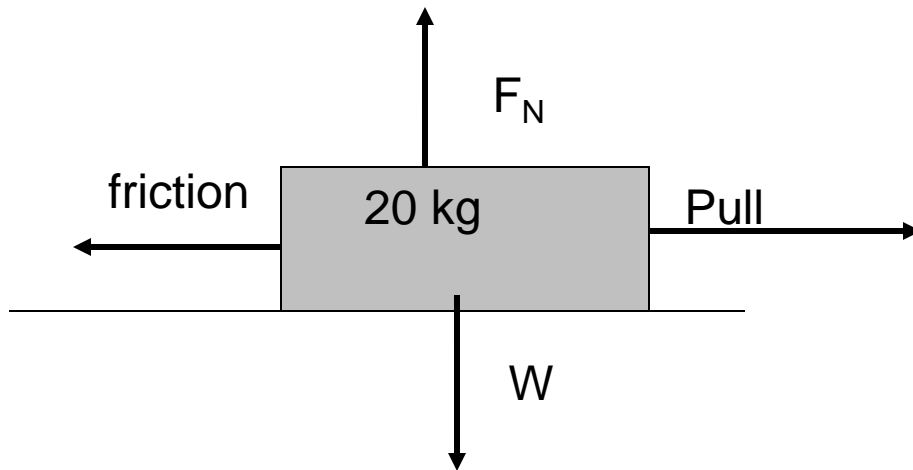


Which one is the correct FBD for an ice puck sliding across frictionless ice?



# Problem solving with 2<sup>nd</sup> Law

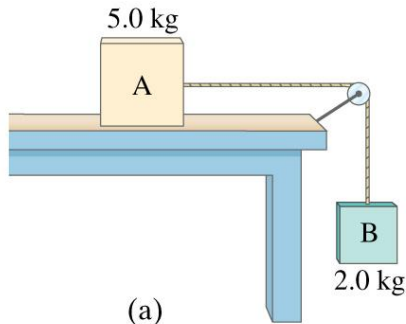
- draw free body diagram
- solve x, y directions independently
- $\Sigma F = ma_x$  Pull + (- friction) =  $ma_x$
- $\Sigma F = ma_y$  Normal force + (- weight) =  $ma_y$
- resolve vectors into components if necessary



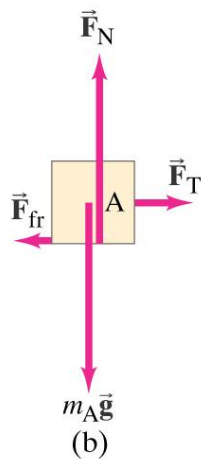
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you may need to use kinematic equations to solve for acceleration or use the acceleration value from above in kinematic equations

# 2 body/pulley problems



(a)



(b)



(c)

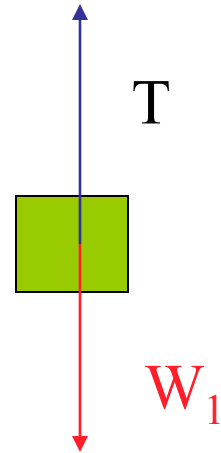
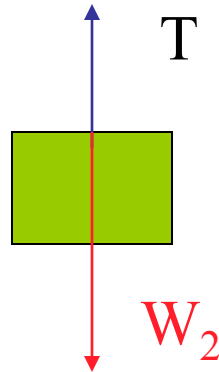
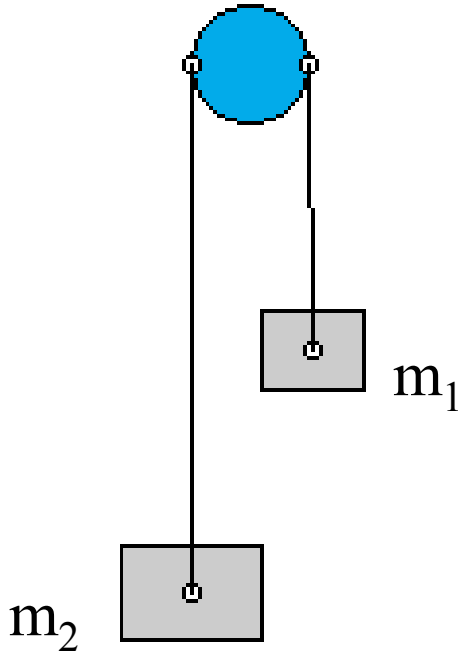
- Apply 2<sup>nd</sup> law to direction of motion – across table and down is + direction, opposite is – direction
- Tension in rope is constant at all points
- Both masses accelerate at same rate
- Must use total mass of system
- Isolate the hanging mass to solve for tension

# Atwood machine

A pulley merely changes the direction of the tension force.

It is easiest to choose a “rotation” direction as + or –

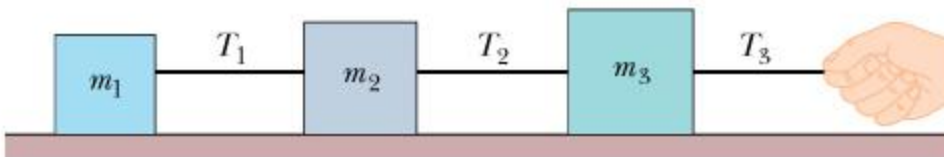
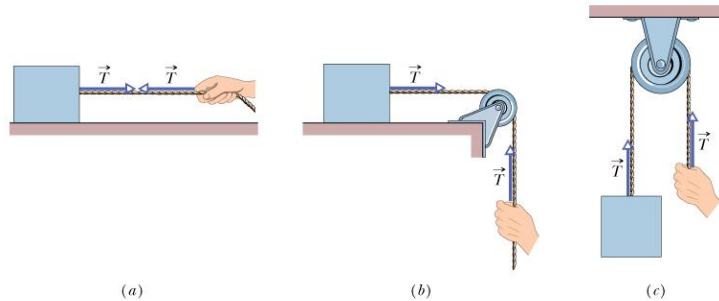
+ up on left, down on right



$$T - W_2 = m_2 a \quad W_1 - T = m_1 a$$

# Tension forces

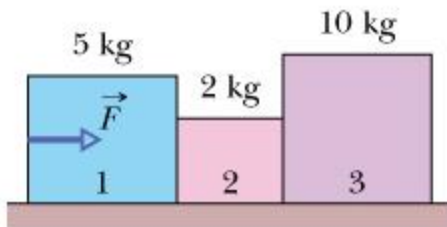
- Created by applying force to a rope, cable
- Equal at all points in rope



Is  $T_1 = T_2 = T_3$ ?

# Multi-body Problems

- NO!
- $\Sigma F = ma$
- All boxes accelerate at same rate
  - applied force is directly proportional to mass that is accelerating



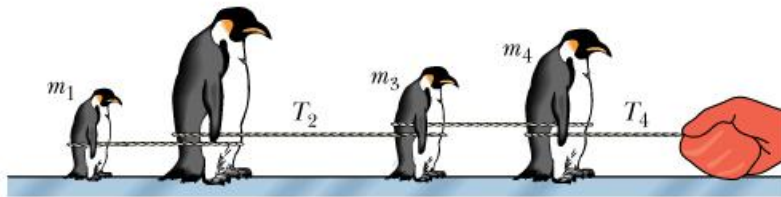
$F = 34 \text{ N}$  to accelerate  $17 \text{ kg}$  at  $2 \text{ m/s}^2$

$$F_2 = 12 \times 2 = 24 \text{ N}$$

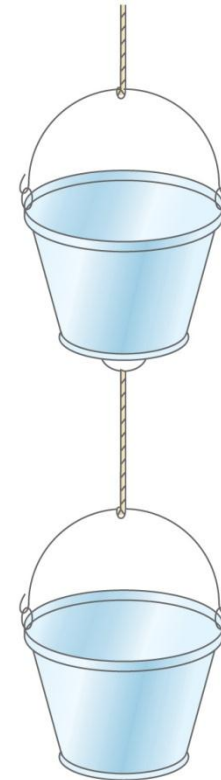
$$F_3 = 10 \times 2 = 20 \text{ N}$$

Example: Thrust force to lift a jet  
much greater than contact force to  
accelerate the pilot in the jet





tension forces between object always less than external pull force

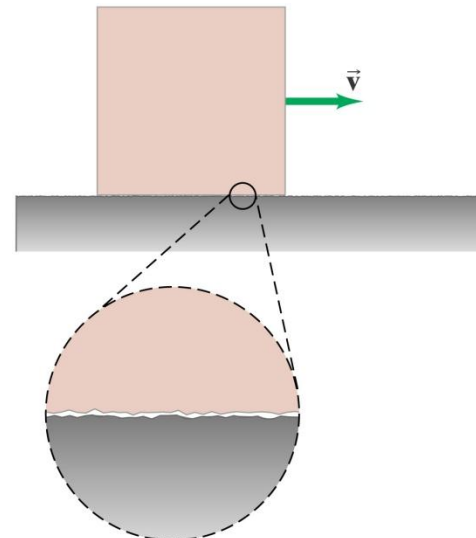
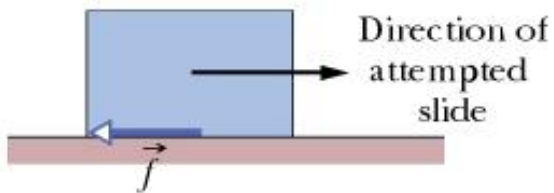


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2 scale demo

# Friction

- Friction forces **ALWAYS** oppose actual or attempted motion between 2 surfaces
- Static friction: no motion  $f_s \leq \mu_s F_N$
- Kinetic friction: sliding motion  $f_k = \mu_k F_N$

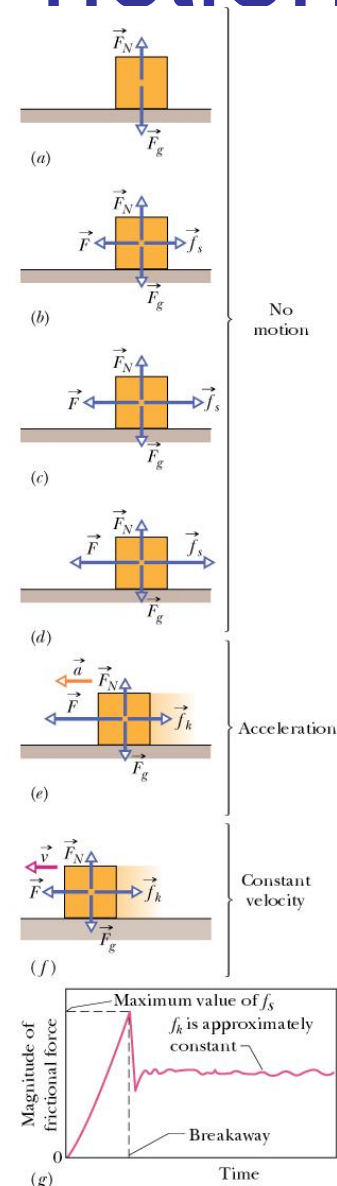


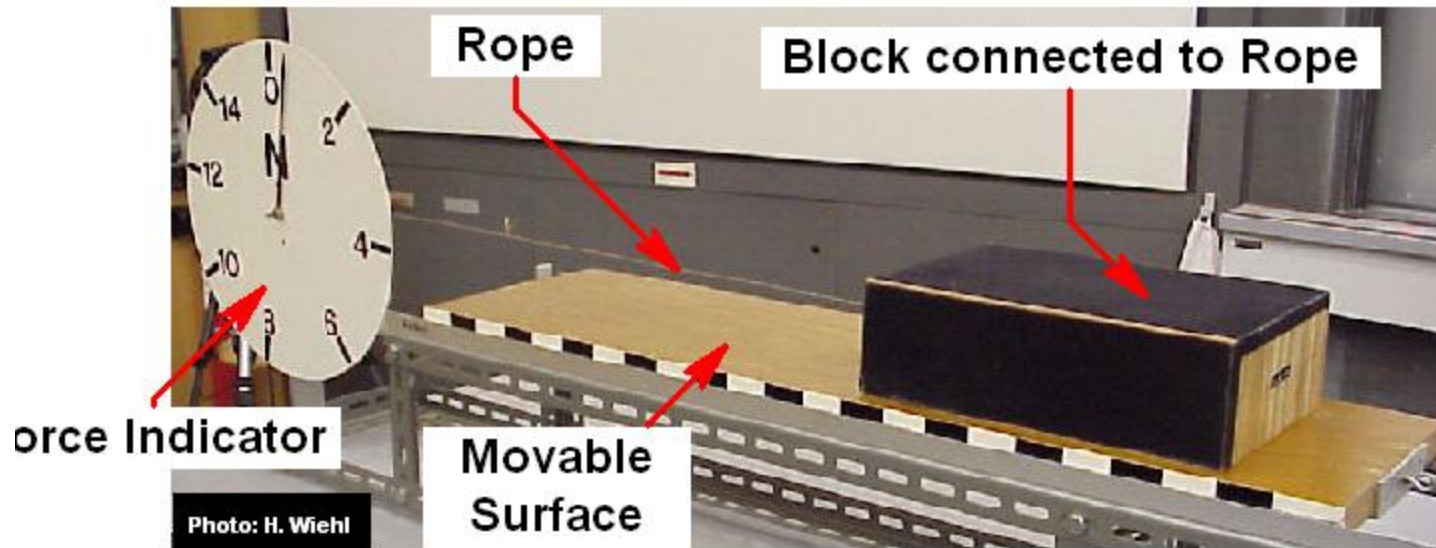
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# Static, Kinetic Friction

- Static friction changes in response to applied force
- Static friction maximum
  - $f_{s,max} = \mu_s F_N$
  - “on the verge of motion”
  - “just started moving”
- Kinetic friction constant
- coefficient of friction  $\mu$  is measure of roughness of two surfaces in contact



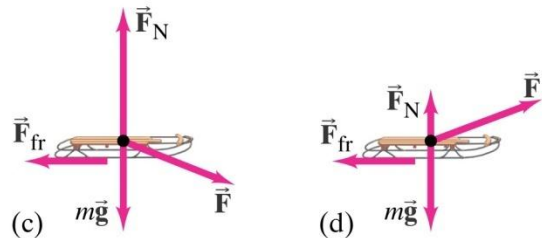
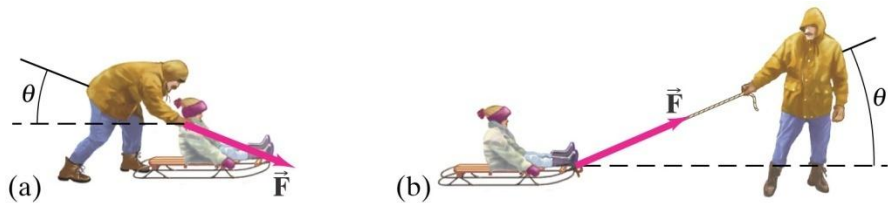


# Sliding Friction

Chapter 1  
Section 2

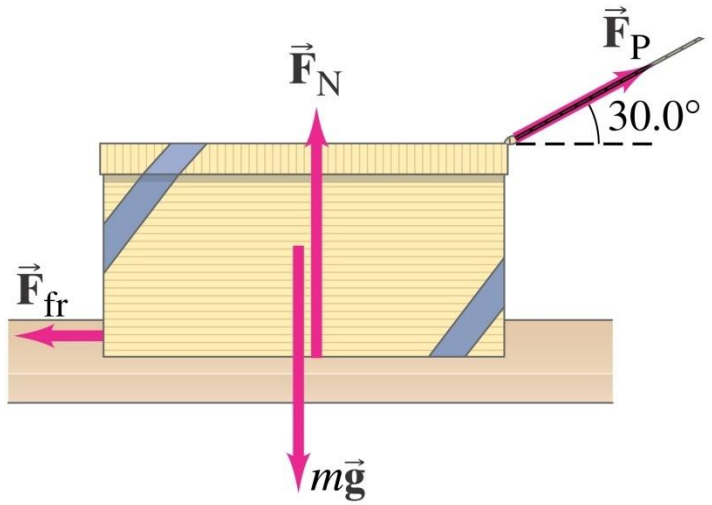
[demo](#)

# Include friction force in free body diagram



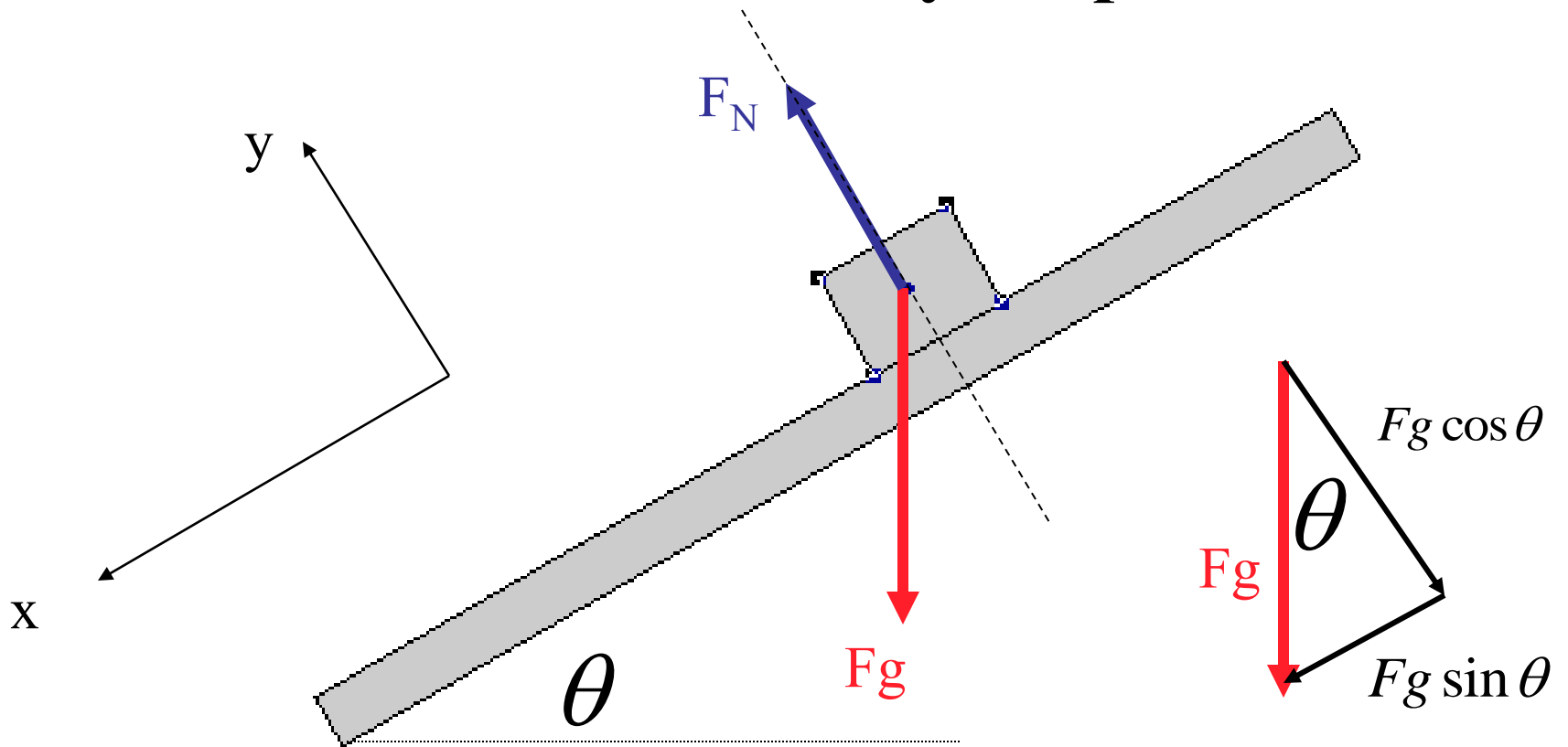
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How does angle affect friction force?



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# Inclines: Which way is up?



Must resolve weight correctly before summing forces in  $x$ ,  $y$

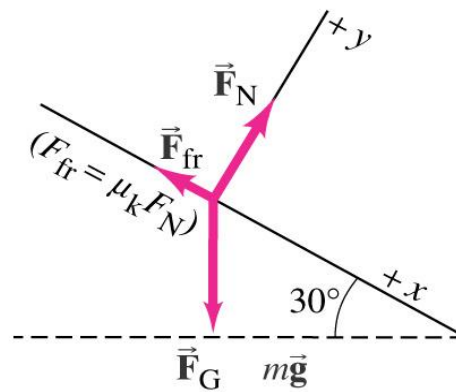
normal force  $F_N$  not equal to weight

# Apply 2<sup>nd</sup> law problem solving techniques

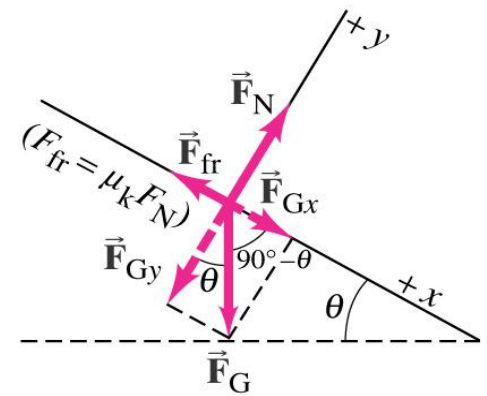
- $\Sigma F_x = ma_x$
- $\Sigma F_y = ma_y$



(a)



(b)



(c)

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